Bucourt, R. \& Hainaut, D. (1965). Bull. Soc. Chim. Fr. pp. 1366-1378.
De Titta, G. T., Edmonds, J. W., Langs, D. A. \& Hauptman, H. (1975). Acta Cryst. A31, 472-479.
Duax, W. L. \& Norton, D. A. (1975). Atlas of Steroid Structure. London: Plenum.
Geise, H. J., Buys, H. R. \& Mijlhoff, F. C. (1971). J. Mol. Struct. 9, 447-452.
Graaff, R. A. G. de \& Romers, C. (1974). Acta Cryst. B30, 2029-2033.
Guy, J. J., Allen, F. H., Kennard, O. \& Sheldrick, G. M. (1977). Acta Cryst. B33, 1236-1244.

Jones, P. G., Falvello, L. \& Kennard, O. (1978). Acta Cryst. B34, 1939-1942.
Potenza, J., Mastropaolo, D., Gallaher, D. \& Henderson, T. (1975). Acta Cryst. B31, 1975-1977.

Roberts, P. J., Pettersen, R. C., Sheldrick, G. M., Isaacs, N. W. \& Kennard, O. (1973). J. Chem. Soc. Perkin Trans. 2, pp. 1978-1984.
Sheldrick, G. M. (1977). Private communication.
Sheldrick, G. M. (1978). In Direct Methods of Solving Crystal Structures. International School of Crystallography, Erice, Italy.
Taylor, I. F., Watson, W. H. \& Smith, W. B. (1976). Cryst. Struct. Commun. 5, 883-890.
Warner, P. M., Lu, S.-L., Myers, E., Dehaven, P. W. \& Jacobson, R. A. (1977). J. Am. Chem. Soc. 99, 51025108.

White, P. S. \& Woolfson, M. M. (1975). Acta Cryst. A31, 53-56.

Acta Cryst. (1979). B35, 2126-2135

# Neutron Diffraction Study of Quinolinic Acid Recrystallized from $\mathbf{D}_{\mathbf{2}} \mathbf{O}$ : Evaluation of Temperature and Isotope Effects in the Structure* 

By Fusao Takusagawa and Thomas F. Koetzle $\dagger$<br>Chemistry Department, Brookhaven National Laboratory, Upton, New York 11973, USA

(Received 15 February 1979; accepted 15 May 1979)


#### Abstract

The structure of quinolinic acid recrystallized from $\mathrm{D}_{2} \mathrm{O}$ (2,3-pyridinedicarboxylic acid; $\mathrm{C}_{7} \mathrm{H}_{3} \mathrm{D}_{2} \mathrm{NO}_{4}$ ) has been refined based on neutron diffraction data measured at four temperatures: $35,80,100$ and 298 K . The principal temperature dependence in cell constants is observed for the $b$ axis, which is perpendicular to the molecular planes. The refined thermal parameters have been extrapolated by a least-squares procedure, to yield values for $T=0 \mathrm{~K}$ which provide estimates of the combined effects of static disorder and zero-point motion. The $D$ atom shifts toward the midpoint of the short intramolecular $\mathrm{O} \cdots \mathrm{O}$ hydrogen bond when the crystal is cooled, just as was found in an earlier study to occur for the H atom in the undeuterated material. At 100 and 298 K , the D atom is displaced significantly further from the bond midpoint than is the H atom at the same temperature. The magnitude of this isotope effect appears to be independent of temperature. The exchangeable protons in the crystal have not been completely replaced by $D$; refinement of the $D$


[^0]scattering lengths indicates the presence of approximately $2 \cdot 7 \% \mathrm{H}$ attached to $\mathrm{N}(1)$ and $4.4 \% \mathrm{H}$ in the short hydrogen bond. The N scattering length has been refined to yield a value of $0.921(2) \times 10^{-11} \mathrm{~mm}$.

## Introduction

The general features of the crystal structure of quinolinic acid with a very short asymmetric intramolecular hydrogen bond have been elucidated from X-ray photographic data by Takusagawa, Hirotsu \& Shimada (1973). Positions of the H atoms, including that in the short hydrogen bond, O...O $2 \cdot 398$ (3) $\AA$, have been confirmed by neutron diffraction techniques at room temperature by Kvick, Koetzle, Thomas \& Takusagawa (1974). Recently we have studied effects of temperature on the crystal structure (Takusagawa \& Koetzle, 1978) and have observed a shift of the H atom toward the midpoint of the $\mathrm{O} \cdots \mathrm{O}$ hydrogen bond upon cooling the crystal to 100 K . We have now refined the structure of quinolinic acid based on neutron diffraction data collected with a sample recrystallized from $\mathrm{D}_{2} \mathrm{O}$. Measurements were made at $35,80,100$ and 298 K , in an attempt to confirm the temperature effects observed in the undeuterated material and in order to elucidate the relationship between temperature and the
effects of $D$ substitution. This work is part of a study of charge-density distributions in quinolinic acid by a combination of X-ray and neutron diffraction techniques.

## Experimental section and data reduction

The sample of quinolinic acid used in this work was recrystallized three times from $\mathrm{D}_{2} \mathrm{O}$. The monoclinic crystal had a volume of $7.9 \mathrm{~mm}^{3}$ and was mounted on an aluminum pin along the crystallographic [103] direction. It was sealed in an aluminum can filled with helium gas.* The can was placed in a closed-cycle helium refrigerator (Air Products and Chemicals, Inc.; DISPLEX ${ }^{\circledR}$ Model CS-202) and mounted on an automated four-circle diffractometer (Dimmler, Greenlaw, Kelley, Potter, Rankowitz \& Stubblefield, 1976; McMullan, Andrews, Koetzle, Reidinger, Thomas \&

[^1]Williams, 1976) at the Brookhaven High Flux Beam Reactor, with a crystal-monochromated neutron beam of wavelength $1.0513 \AA$ (based upon $\mathrm{KBr}, a=6.600$ $\AA$ at 298 K ). The temperatures recorded during data collection were $35 \pm 0 \cdot 5,80 \pm 0 \cdot 5,100 \pm 0 \cdot 5^{*}$ and $298 \pm 3 \mathrm{~K}$. Cell dimensions refined by a least-squares procedure based on setting angles of 29 reflections are listed in Table 1. Intensities were measured for reflections comprising two octants of reciprocal space ( $h k l, h k \bar{l}$ ) and portions of two additional octants ( $h \bar{k} l$ and $h \bar{k} \bar{l}$ ). A $\theta / 2 \theta$ step-scan technique was employed, with the scan range varied according to $\Delta 2 \theta=1.98^{\circ}$ $\times(1.0+2.98 \tan \theta)$ for the high-angle data $\left(2 \theta \geq 50^{\circ}\right)$, and $\Delta 2 \theta=4.0^{\circ}$ for the low-angle data. The step size was adjusted to give approximately 66 points in each scan. As a general check on experimental stability, the intensities of two reflections were remeasured every 100 reflections. These did not vary to any significant degree during the entire period of data collection at any given

[^2]Table 1. Crystal data for quinolinic acid
2,3-Pyridinedicarboxylic acid, $\mathrm{C}_{7} \mathrm{H}_{3} \mathrm{D}_{2} \mathrm{NO}_{4}$ (D-QNA), $M_{r}=169 \cdot 11$, space group $P 2_{1} / c, Z=4$.
Cell constants and linear absorption coefficients

|  | $35 \mathrm{~K}(\mathrm{D})$ | $80 \mathrm{~K}(\mathrm{D})$ | $100 \mathrm{~K}(\mathrm{D})$ | $100 \mathrm{~K}(\mathrm{H})^{*}$ | $298 \mathrm{~K}(\mathrm{D}) \dagger$ | $298 \mathrm{~K}(\mathrm{H}) \ddagger$ |
| :--- | :---: | :---: | :---: | :---: | ---: | ---: |
| $a(\AA)$ | $7.420(2)$ | $7.420(2)$ | $7.422(2)$ | $7.414(1)$ | $7.421(1)$ | $7.422(1)$ |
| $b(\AA)$ | $12.308(4)$ | $12.366(4)$ | $12.392(4)$ | $12.389(2)$ | $12.695(2)$ | $12.705(2)$ |
| $c(\AA)$ | $7.831(4)$ | $7.833(4)$ | $7.835(5)$ | $7.832(1)$ | $7.831(1)$ | $7.834(1)$ |
| $\beta\left(^{\circ}\right)$ | $117.06(2)$ | $117.06(2)$ | $117.06(2)$ | $117.05(1)$ | $116.96(2)$ | $116.95(1)$ |
| $\bar{V}\left(\AA^{3}\right)$ | $636.9(4)$ | $640.0(4)$ | $641.7(4)$ | $640.7(2)$ | $657.6(2)$ | $658.5(2)$ |
| $\mu \S\left(\mathrm{mm}^{-1}\right)$ | 0.0763 | 0.0758 | 0.0755 | 0.1247 | 0.0737 | 0.1227 |

* By X-rays (Mo $K\left(r_{1}, \lambda=0.70926 \AA\right.$ ) (Kvick, 1978).
$\dagger$ By X-rays $(\mathrm{Cu} \mathrm{Kar}, \lambda=1.5405 \AA$ ) .
$\ddagger$ By X-rays $\left(\mathrm{Cr} K a_{1}, \lambda=2 \cdot 2896 \AA\right.$ ) (Kvick et al., 1974).
§ The effective absorption cross section for incoherent scattering of H was taken to be 40 barn ( $4000 \mathrm{fm}^{2}$ ).

Table 2. Experimental and refinement parameters (conventional refinement with anisotropic thermal parameters)

| Crystal weight | 13.5 mg |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Crystal volume at room temperature | $7.9 \mathrm{~mm}^{3}$ |  |  |  |
| Number of faces | 13 |  |  |  |
|  | 35 K | 80 K | 100 K | 298 K |
| Number of reflections measured | 2415 | 1745 | 1747 | 2735 |
| Agreement factor on averaging ( $\left.R_{c}\right)^{*}$ | 0.015 | 0.017 | 0.017 | 0.031 |
| Number of independent reflections | 1694 | 1533 | 1534 | 2191 |
| Range of $\sin \theta / \lambda\left(\AA^{-1}\right)$ | $0.0 \sim 0.71$ | $0.0 \sim 0.66$ | $0.0 \sim 0.66$ | $0.0 \sim 0.73$ |
| $R\left(F^{2}\right)=\sum\left\|F_{o}^{2}-k^{2} F_{c}^{2}\right\| / \sum F_{o}^{2}$ | 0.032 | 0.032 | 0.032 | 0.046 |
| $w R\left(F^{2}\right)=\left(\sum w\left\|F_{o}^{2}-k^{2} F_{c}^{2}\right\| / \sum w F_{o}^{4}\right)^{1 / 2}$ | 0.053 | 0.053 | 0.054 | 0.085 |
| $S \dagger=\left[\sum w\left\|F_{o}^{2}-k^{2} F_{c}^{2}\right\|^{2 /}(m-n)\right]^{1 / 2}$ | 1.55 | 1.50 | 1.54 | 1.83 |
| $R_{c}=\sum\left(\sum_{l=1}^{n^{\prime}} \mid\left\langle F_{o}^{2}\right\rangle-F_{o_{l}}^{2}\right) / \sum n^{\prime}\left\langle F_{o}^{2}\right\rangle$ | is the num | equivalent | ations for | eflection. |
| $\dagger m$ is the number of reflections and $n$ is | ne number of | able parame | 158). |  |

## 2128 NEUTRON DIFFRACTION OF QUINOLINIC ACID RECRYSTALLIZED FROM $\mathrm{D}_{2} \mathrm{O}$

temperature. Experimental quantities of interest are listed in Table 2 along with some details of the subsequent refinements.

Integrated intensities of reflections were obtained by a method described earlier (Takusagawa \& Koetzle, 1978). Absorption corrections for observed intensities were calculated by a modification of the analytical method of de Meulenaer \& Tompa (1965) (Alcock, 1970; Templeton \& Templeton, 1973). The variance of the net intensity of each reflection was estimated as follows: $\sigma^{2}(I)=T+B+[0.03(T-B)]^{2}+(0.03 B)^{2}$ $+C$, where $T$ and $B$ are total and background counts, respectively, and the factor 0.03 represents an estimate of non-Poisson errors. The constant $C$ was adjusted to yield a uniform value of $\left\langle\Delta F^{2} / \sigma\left(F^{2}\right)\right\rangle$ in all regions of $F^{2}$ upon completion of the refinements. Final values of $C$ on an absolute scale in units of $10^{-22} \mathrm{~mm}^{2}$ are 5.6 (35 K), $4 \cdot 7(80 \mathrm{~K}), 4 \cdot 1(100 \mathrm{~K})$ and $0 \cdot 0(298 \mathrm{~K})$. Squared observed structure factors were obtained as $F_{o}^{2}=I \times$ $\sin 2 \theta$ and averaged for symmetry-related reflections (agreement factors are included in Table 2).

## Structure refinement

The atomic coordinates from the neutron diffraction study of Takusagawa \& Koetzle (1978) were used as initial values for a full-matrix least-squares refinement minimizing $\sum w\left(F_{o}^{2}-k^{2} F_{c}^{2}\right)$ and using a modification of the program by Busing, Martin \& Levy (1962). Weights were chosen as $w=1 / \sigma^{2}\left(F^{2}\right)=1 /\left[\sigma^{2}(I) \times\right.$ $\sin ^{2} 2 \theta$ ]. Positional and anisotropic thermal parameters were varied for all atoms together with a scale factor, $k$, the coherent neutron scattering length of D and N atoms, and a type (I) isotropic extinction correction parameter (Becker \& Coppens, 1975). A correction was applied for the effects of a small number of neutrons in the incident beam with wavelength $\lambda / 2$, by means of a least-squares procedure, minimizing $\sum w\left[\left(1 / k^{2}\right) F_{o}^{2}(h k l)-F_{c}^{2}(h k l)-k^{\prime} F_{c}^{2}(2 h 2 k 2 l)\right]^{2}$. The values of $k^{\prime}$ obtained are 0.0021 (5) for 35 K , 0.0028 (5) for $80 \mathrm{~K}, 0.0031$ (5) for 100 K and 0.0019 (5) for 298 K . Final positional and thermal parameters obtained from refinements performed after correction for the $\lambda / 2$ component are listed in Table 3.*

Rigid-body analyses, the results of which will be discussed below in some detail, indicate large librational motions around the $\mathrm{C}-\mathrm{C}$ bonds of the carboxyl groups. Therefore, in order to investigate the possible significance of curvilinear or anharmonic motion, thirdand fourth-order thermal tensors for the four O atoms and the D in the intramolecular hydrogen bond were

[^3]refined using the expansion developed by Johnson (1970a,b). A summary of these refinements is given in Table 4. Based on the $R$-value test (Hamilton, 1965), the fit of the model to the observed data was judged to be improved significantly only for the 298 K study. In any event, the positional parameters were essentially identical to those obtained in the conventional refinements. Neutron scattering lengths used (all $\times 10^{-11}$ $\mathrm{mm})$ are $b_{C}=0.665$ (Bacon, 1972), $b_{\mathrm{H}}=-0.374, b_{\mathrm{O}}=$ $0.580, b_{\mathrm{D}}=0.6672$ (Shull, 1972), and $b_{\mathrm{N}}=0.921$ (2). As noted above, the value for N was refined, along with the effective scattering length for D which was used as a measure of the extent of deuteration.

## Discussion

The general features of the structure have been treated in detail in earlier papers (Takusagawa et al., 1973; Kvick et al., 1974). The present discussion will mainly be restricted to those aspects of the structure which are observed to change with temperature, and the effects of

(a)

(c)

(b)

(d)

Fig. 1. Molecular views of D-QNA at (a) $35 \mathrm{~K},(b) 80 \mathrm{~K}$, (c) 100 K, and (d) 298 K . Thermal ellipsoids are drawn at the $97 \%$ probability level.


Fig. 2. Bond distances $(\AA)$ at 35 K . The differences, $\Delta D(T)=D(T)$ $-D(35)$, for $T=80,100$, and 298 K , respectively, are given in parentheses below the values at 35 K . Estimated standard deviations are $0.002 \sim 0.003 \AA$.

Table 3. Positional and thermal parameters from the conventional refinement
Thermal parameters are of the form $\exp \left[-2 \pi^{2}\left(h^{2} a^{* 2} U_{11}+\ldots+2 h k a^{*} b^{*} U_{12}+\ldots\right)\right]$.

| $\mathrm{N}(1) 298 \mathrm{~K}$ | 0.93600 (8) | $0 \cdot 12237$ (6) | $0 \cdot 10547$ (8) | 0.0154 (3) | 0.0440 (4) | 0.0199 (3) | 0.0011 (2) | 0.0103 (2) | 0.0006 (2) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 | 0.93732 (7) | $0 \cdot 12241$ (4) | $0 \cdot 10789$ (6) | 0.0071 (2) | 0.0142 (3) | 0.0072 (2) | 0.0003 (2) | 0.0043 (2) | -0.0001 (1) |
| 80 | 0.93747 (7) | $0 \cdot 12242$ (4) | $0 \cdot 10803$ (6) | 0.0063 (2) | 0.0122 (2) | 0.0060 (2) | 0.0004 (2) | 0.0037 (2) | 0.0001 (1) |
| 35 | 0.93772 (6) | $0 \cdot 12241$ (3) | $0 \cdot 10840$ (6) | 0.0047 (2) | 0.0084 (2) | 0.0042 (2) | 0.0002 (1) | 0.0026 (2) | -0.0001 (1) |
| C(2)298 | 0.7342 (1) | $0 \cdot 12462$ (7) | -0.0042 (1) | 0.0167 (3) | 0.0337 (4) | 0.0159 (3) | 0.0005 (3) | 0.0089 (2) | 0.0002 (3) |
| 100 | 0.73464 (9) | $0 \cdot 12461$ (5) | -0.00241 (8) | 0.0081 (3) | 0.0115 (3) | 0.0063 (2) | 0.0004 (2) | 0.0039 (2) | 0.0004 (2) |
| 80 | 0.73477 (9) | $0 \cdot 12458$ (5) | -0.00221 (9) | 0.0073 (3) | 0.0100 (3) | 0.0054 (2) | 0.0000 (2) | 0.0034 (2) | 0.0001 (2) |
| 35 | 0.73495 (8) | $0 \cdot 12459$ (5) | -0.00198 (8) | 0.0052 (2) | 0.0071 (2) | 0.0039 (2) | 0.0004 (2) | 0.0024 (2) | 0.0005 (2) |
| C(3)298 | 0.6111 (1) | $0 \cdot 12623$ (7) | 0.0877 (1) | 0.0143 (3) | 0.0331 (4) | 0.0180 (3) | 0.0001 (3) | 0.0087 (2) | -0.0001 (3) |
| 100 | 0.61138 (9) | $0 \cdot 12623$ (5) | 0.09003 (8) | 0.0067 (3) | 0.0113 (3) | 0.0069 (3) | 0.0001 (2) | 0.0034 (2) | -0.0003 (2) |
| 80 | 0.61162 (9) | $0 \cdot 12624$ (5) | $0 \cdot 09027$ (8) | 0.0065 (3) | 0.0098 (3) | 0.0061 (3) | 0.0002 (2) | 0.0033 (2) | -0.0002 (2) |
| 35 | 0.61169 (8) | $0 \cdot 12620$ (5) | $0 \cdot 09055$ (8) | 0.0043 (2) | 0.0072 (2) | 0.0039 (2) | 0.0001 (2) | 0.0018 (2) | -0.0002 (2) |
| C(4)298 | 0.7051 (1) | $0 \cdot 12251$ (8) | 0.2887 (1) | 0.0211 (3) | 0.0430 (5) | 0.0181 (3) | 0.0004 (3) | 0.0112 (3) | 0.0001 (3) |
| 100 | 0.7058 (1) | $0 \cdot 12212$ (5) | 0.29122 (8) | 0.0092 (3) | 0.0140 (3) | 0.0070 (3) | -0.0000 (2) | 0.0045 (2) | -0.0001 (2) |
| 80 | 0.7060 (1) | $0 \cdot 12210$ (5) | 0.29154 (8) | 0.0082 (3) | 0.0119 (3) | 0.0061 (3) | 0.0001 (2) | 0.0039 (2) | 0.0001 (2) |
| 35 | 0.70630 (8) | $0 \cdot 12197$ (5) | 0.29201 (8) | 0.0053 (2) | 0.0085 (2) | 0.0043 (3) | -0.0001 (2) | 0.0024 (2) | 0.0000 (2) |
| C(5)298 | 0.9135 (1) | $0 \cdot 12139$ (9) | 0.3942 (1) | 0.0220 (3) | 0.0505 (5) | 0.0163 (3) | 0.0018 (4) | 0.0081 (3) | 0.0009 (4) |
| 100 | 0.9151 (1) | $0 \cdot 12134$ (5) | 0.39742 (9) | 0.0090 (3) | 0.0165 (3) | 0.0060 (3) | 0.0007 (2) | 0.0033 (2) | 0.0006 (2) |
| 80 | 0.9153 (1) | $0 \cdot 12134$ (5) | 0.39778 (9) | 0.0082 (3) | 0.0139 (3) | 0.0050 (3) | 0.0008 (2) | 0.0028 (2) | 0.0005 (2) |
| 35 | 0.91572 (9) | $0 \cdot 12129$ (5) | 0.39833 (8) | 0.0058 (2) | 0.0098 (2) | 0.0032 (2) | 0.0003 (2) | 0.0017 (2) | 0.0004 (2) |
| C(6)298 | 1.0286 (1) | $0 \cdot 12201$ (9) | 0.2963 (1) | 0.0168 (3) | 0.0504 (5) | 0.0198 (3) | 0.0015 (3) | 0.0069 (3) | 0.0009 (4) |
| 100 | 1.0306 (1) | $0 \cdot 12201$ (6) | 0.29923 (9) | 0.0083 (3) | 0.0166 (3) | 0.0071 (3) | 0.0005 (2) | 0.0036 (2) | 0.0003 (2) |
| 80 | 1.0307 (1) | $0 \cdot 12208$ (6) | 0.29939 (9) | 0.0076 (3) | 0.0141 (3) | 0.0060 (3) | 0.0006 (2) | 0.0031 (2) | 0.0003 (2) |
| 35 | 1.03101 (8) | $0 \cdot 12212$ (5) | $0 \cdot 29987$ (8) | 0.0057 (2) | 0.0097 (3) | 0.0043 (3) | 0.0004 (2) | 0.0023 (2) | $0 \cdot 0002$ (2) |
| C(7)298 | 0.6816 (1) | $0 \cdot 12152$ (9) | -0.2181 (1) | 0.0248 (4) | 0.0460 (5) | 0.0174 (3) | -0.0011 (3) | 0.0117 (3) | -0.0004 (3) |
| 100 | 0.6820 (1) | $0 \cdot 12101$ (5) | -0.21659 (8) | 0.0103 (3) | 0.0155 (3) | 0.0064 (2) | -0.0001 (2) | 0.0041 (2) | $0 \cdot 0001$ (2) |
| 80 | $0 \cdot 6820$ (1) | $0 \cdot 12103$ (5) | -0.21652 (8) | 0.0090 (3) | 0.0128 (3) | 0.0059 (2) | -0.0002 (2) | 0.0038 (2) | -0.0000 (2) |
| 35 | 0.68206 (9) | $0 \cdot 12094$ (5) | -0.21636 (8) | 0.0062 (2) | 0.0083 (2) | 0.0041 (2) | -0.0000 (2) | 0.0027 (2) | 0.0000 (2) |
| C(8)298 | 0.3823 (1) | $0 \cdot 13305$ (8) | -0.0064 (1) | 0.0158 (3) | 0.0416 (5) | 0.0266 (4) | -0.0009 (3) | 0.0109 (3) | -0.0018 (3) |
| 100 | $0 \cdot 38224$ (9) | $0 \cdot 13385$ (5) | -0.00448 (9) | 0.0081 (3) | 0.0136 (3) | 0.0093 (3) | -0.0004 (2) | 0.0052 (2) | -0.0002 (2) |
| 80 | $0 \cdot 38217$ (9) | $0 \cdot 13393$ (5) | -0.00430 (9) | $0 \cdot 0072$ (3) | 0.0115 (3) | 0.0078 (3) | -0.0004 (2) | 0.0045 (2) | -0.0006 (2) |
| 35 | $0 \cdot 38227$ (8) | $0 \cdot 13412$ (5) | -0.00387 (8) | 0.0055 (2) | 0.0076 (2) | 0.0054 (3) | -0.0004 (2) | 0.0033 (2) | -0.0003 (2) |
| O(1)298 | 0.8228 (2) | 0.1080 (1) | -0.2538 (2) | 0.0345 (6) | 0.088 (1) | 0.0254 (5) | 0.0019 (6) | 0.0213 (4) | -0.0008 (6) |
| 100 | 0.8240 (1) | 0. 10685 (7) | -0.2525 (1) | 0.0138 (3) | 0.0271 (4) | 0.0094 (3) | 0.0006 (3) | 0.0079 (3) | -0.0002 (3) |
| 80 | 0.8241 (1) | 0.10682 (7) | -0.2525 (1) | 0.0120 (3) | 0.0226 (4) | 0.0081 (3) | 0.0006 (3) | 0.0067 (2) | -0.0002 (3) |
| 35 | $0 \cdot 8245$ (1) | 0.10664 (6) | -0.2523 (1) | 0.0081 (3) | 0.0148 (3) | 0.0061 (3) | 0.0007 (2) | 0.0046 (2) | 0.0001 (2) |
| O(2)298 | 0.4993 (2) | $0 \cdot 1354$ (1) | -0.3394 (1) | 0.0281 (5) | 0.079 (1) | 0.0173 (4) | 0.0026 (5) | 0.0065 (4) | 0.0042 (5) |
| 100 | 0.4980 (1) | 0.13498 (7) | -0.3390 (1) | 0.0114 (4) | 0.0250 (4) | 0.0066 (3) | 0.0009 (3) | 0.0026 (3) | 0.0012 (3) |
| 80 | 0.4977 (1) | $0 \cdot 13487$ (7) | -0.3389 (1) | 0.0103 (3) | 0.0204 (4) | 0.0056 (3) | 0.0008 (3) | 0.0025 (3) | 0.0010 (3) |
| 35 | 0.4976 (1) | $0 \cdot 13487$ (6) | -0.3388 (1) | 0.0066 (3) | 0.0135 (3) | 0.0042 (3) | 0.0006 (2) | 0.0018 (2) | 0.0005 (2) |
| O(3)298 | 0.2863 (2) | 0.1528 (1) | -0.1855 (2) | 0.0175 (4) | 0.093 (1) | 0.0284 (5) | 0.0034 (5) | 0.0059 (4) | 0.0078 (6) |
| 100 | 0.2853 (1) | $0 \cdot 15540$ (7) | -0.1843 (1) | 0.0086 (3) | 0.0296 (4) | 0.0094 (3) | 0.0010 (3) | 0.0032 (3) | 0.0023 (3) |
| 80 | 0.2852 (1) | $0 \cdot 15557$ (7) | -0.1842 (1) | 0.0079 (3) | 0.0245 (4) | 0.0078 (3) | 0.0012 (3) | 0.0029 (3) | 0.0021 (3) |
| 35 | 0.2853 (1) | $0 \cdot 15600$ (6) | -0.1841 (1) | 0.0057 (3) | 0.0157 (3) | 0.0051 (3) | 0.0007 (2) | 0.0023 (2) | 0.0012 (2) |
| O(4)298 | 0.2983 (2) | $0 \cdot 1198$ (1) | 0.0943 (2) | 0.0210 (4) | 0.0755 (9) | 0.0365 (5) | -0.0017 (5) | 0.0192 (4) | 0.0004 (6) |
| 100 | 0.2979 (1) | $0 \cdot 12010$ (7) | 0.0973 (1) | 0.0095 (3) | 0.0241 (4) | 0.0125 (3) | -0.0011 (3) | 0.0072 (3) | 0.0002 (3) |
| 80 | $0 \cdot 2980$ (1) | $0 \cdot 12007$ (7) | 0.0975 (1) | 0.0088 (3) | 0.0198 (4) | 0.0105 (3) | -0.0007 (3) | 0.0063 (2) | 0.0004 (3) |
| 35 | 0.2982 (1) | $0 \cdot 12018$ (6) | 0.0980 (1) | 0.0063 (3) | 0.0131 (3) | 0.0068 (3) | -0.0005 (2) | 0.0043 (2) | 0.0005 (2) |
| H(1)298 | 0.6109 (3) | 0.1214 (2) | 0.3612 (3) | 0.0373 (9) | 0.088 (2) | 0.0359 (9) | $0 \cdot 002$ (1) | 0.0251 (8) | 0.001 (1) |
| 100 | 0.6120 (2) | $0 \cdot 1207$ (1) | 0.3641 (2) | 0.0229 (7) | 0.0408 (8) | 0.0208 (6) | $0 \cdot 0004$ (6) | 0.0153 (5) | 0.0001 (6) |
| 80 | 0.6122 (2) | $0 \cdot 1206$ (1) | 0.3647 (2) | 0.0220 (7) | 0.0387 (8) | 0.0199 (6) | 0.0004 (6) | 0.0148 (5) | -0.0001 (6) |
| 35 | 0.6123 (2) | $0 \cdot 1204$ (1) | 0.3650 (2) | 0.0184 (5) | 0.0337 (7) | 0.0178 (6) | 0.0002 (5) | 0.0129 (5) | -0.0001 (5) |
| H(2)298 | 0.9844 (3) | $0 \cdot 1202$ (3) | 0.5492 (3) | 0.041 (1) | 0.092 (2) | 0.0222 (7) | 0.005 (1) | 0.0102 (7) | 0.002 (1) |
| 100 | 0.9862 (2) | 0.1201 (1) | 0.5527 (2) | 0.0247 (7) | 0.0421 (8) | 0.0118 (6) | 0.0016 (6) | 0.0064 (5) | 0.0014 (6) |
| 80 | 0.9864 (2) | 0.1202 (1) | 0.5530 (2) | 0.0230 (7) | 0.0389 (8) | 0.0112 (6) | 0.0014 (6) | 0.0063 (5) | 0.0011 (6) |
| 35 | 0.9869 (2) | 0.1205 (1) | 0.5537 (2) | 0.0198 (6) | 0.0328 (7) | 0.0090 (5) | 0.0017 (5) | 0.0049 (5) | 0.0013 (5) |
| H(3)298 | 1.1921 (3) | $0 \cdot 1210$ (3) | 0.3644 (3) | 0.0222 (8) | 0.097 (2) | 0.0376 (9) | $0 \cdot 002$ (1) | 0.0082 (7) | 0.001 (1) |
| 100 | 1-1945 (2) | 0.1213 (1) | 0.3670 (2) | 0.0151 (6) | 0.0443 (9) | 0.0206 (6) | 0.0006 (6) | 0.0056 (5) | 0.0012 (6) |
| 80 | $1 \cdot 1950$ (2) | 0.1213 (1) | 0.3674 (2) | 0.0146 (6) | 0.0402 (8) | 0.0197 (6) | $0 \cdot 0003$ (6) | 0.0057 (5) | 0.0008 (6) |
| 35 | 1-1954 (2) | 0.1213 (1) | 0.3676 (2) | 0.0117 (5) | 0.0338 (7) | 0.0171 (6) | 0.0002 (5) | 0.0049 (4) | 0.0008 (5) |
| D(4)298 | 1.0266 (2) | $0 \cdot 1204$ (1) | 0.0354 (2) | 0.0269 (5) | 0.0628 (8) | 0.0359 (6) | 0.0019 (4) | 0.0213 (4) | 0.0009 (5) |
| 100 | 1.0285 (1) | 0.12048 (7) | 0.0375 (1) | 0.0151 (4) | 0.0279 (5) | 0.0176 (4) | 0.0007 (3) | 0.0107 (3) | 0.0007 (3) |
| 80 | 1.0287 (1) | 0.12045 (7) | 0.0378 (1) | 0.0144 (4) | 0.0243 (4) | 0.0166 (4) | 0.0007 (3) | 0.0102 (3) | 0.0005 (3) |
| 35 | 1.0289 (1) | $0 \cdot 12045$ (6) | 0.0381 (1) | 0.0126 (3) | 0.0199 (4) | 0.0136 (4) | 0.0007 (2) | 0.0085 (3) | 0.0006 (3) |
| D(5)298 | 0.3861 (2) | 0.1483 (1) | -0.2609 (2) | 0.0299 (6) | 0.088 (1) | 0.0288 (6) | $0 \cdot 0005$ (6) | 0.0049 (4) | 0.0079 (6) |
| 100 | 0.3862 (1) | 0.14958 (8) | -0.2601 (1) | 0.0166 (4) | 0.0331 (5) | 0.0153 (4) | 0.0005 (3) | 0.0036 (3) | 0.0030 (3) |
| 80 | 0.3860 (1) | 0.14981 (8) | -0.2601 (1) | 0.0156 (4) | 0.0289 (5) | 0.0136 (4) | 0.0007 (3) | 0.0033 (3) | 0.0029 (3) |
| 35 | 0.3861 (1) | $0 \cdot 15004$ (7) | -0.2599 (1) | 0.0128 (4) | 0.0213 (4) | 0.0116 (4) | $0 \cdot 0004$ (3) | 0.0028 (3) | 0.0021 (3) |

## 2130 NEUTRON DIFFRACTION OF QUINOLINIC ACID RECRYSTALLIZED FROM $\mathrm{D}_{2} \mathrm{O}$

D substitution upon the geometry of the hydrogen bonds.

The molecular structure of D-QNA* in the crystalline state at $35,80,100$ and 298 K is illustrated in Fig. 1 (Johnson, 1976), and bond distances and angles are shown in Figs. 2 and 3 respectively. Differences in bond distances between D-QNA and H-QNA (Kvick et al., 1974; Takusagawa \& Koetzle, 1978) are presented in Fig. 4

## Temperature effects in D-QNA

The effects of cooling on the structure are very similar to those observed in H-QNA (Takusagawa \&

[^4]Table 4. Summary of refinements incorporating thirdand fourth-order thermal tensors for $\mathrm{O}(1), \mathrm{O}(2), \mathrm{O}(3)$, $\mathrm{O}(4)$ and $\mathrm{D}(5)$

|  |  | $\omega R\left(F^{2}\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Temperature | $m$ | (I)* | (II) $\dagger$ | (III) $\ddagger$ | (IV)§ |
| 35 K | 1694 | 0.053 | 0.051 | - | $0.053(159)$ |
| 80 | 1533 | 0.053 | 0.051 | - | $0.052(161)$ |
| 100 | 1534 | 0.054 | 0.053 | - | $0.053(163)$ |
| 298 | 2191 | 0.085 | 0.081 | 0.080 | $0.083(163)$ |

* Conventional refinement, with second-order thermal tensors ( $n=158$ ).
$\dagger$ Refinement including third-order thermal tensors ( $n=208$ ).
$\ddagger$ Refinement including third- and fourth-order thermal tensors ( $n=283$ ). Fourth-order coefficients did not converge owing to very high correlations with second-order terms, except for the 298 K data.
§Refinements in which the values of all third- and fourthorder coefficients having magnitudes less than $3 \sigma$ have been set equal to 0 ( $n$ given in parentheses).


Fig. 3. Bond angles $\left({ }^{\circ}\right)$ at 35 K . The differences, $\Delta A(T)=A(T)-$ $A(35)$, for $T=80,100$ and 298 K , respectively, are given in parentheses below the values at 35 K . Estimated standard deviations are $0.1^{\circ}$ except $0.1 \sim 0.2^{\circ}$ for $\mathrm{O}(2)-\mathrm{D}(5)-\mathrm{O}(3)$.

Koetzle, 1978). The principal change in cell dimensions is observed for the crystallographic $b$ axis, which is perpendicular to the molecular planes (refer to Table 1). There is no hydrogen bonding between these molecular sheets (Takusagawa et al., 1973; Kvick et al., 1974), which interact only by means of van der Waals forces. No significant change with temperature is observed in the $a$ and $c$ axes, i.e. within molecular sheets. The relationship between temperature and the length of the $b$ axis for D-QNA is quite linear, as illustrated in Fig. 5. The calculated linear-expansion coefficient, $\beta$, is $1.19 \times 10^{-4} \mathrm{~K}^{-1}$. Results of rigid-body thermal-motion analyses carried out by the method of Schomaker \& Trueblood (1968) are summarized in Table 5 and indicate that the largest translational tensor component at 298 K is perpendicular to the molecular planes $\left(T_{z}\right)$. $\mathbf{S}$ tensor components were in all cases quite small: the largest effective screw translation is calculated to be $0.006 \AA$. All translational and librational tensor components are markedly reduced when the crystal is cooled, as expected. In particular, the large decrease in $T_{Z}$ together with that in $L_{X}$ and $L_{Y}$, and the resulting decrease in amplitude of out-ofplane motion allows shorter van der Waals contacts between the molecular planes and is in turn related to the decrease in the $b$-axis repeat.


Fig. 4. Isotope effects on bond distances at 100 and 298 K . The values shown are Diff. $(100 \mathrm{~K})=\mathrm{D}(100 \mathrm{~K})-\mathrm{H}(100 \mathrm{~K})$ and Diff. $(298 \mathrm{~K})=\mathrm{D}(298 \mathrm{~K})-\mathrm{H}(298 \mathrm{~K})$. The value at 100 K is shown above that at 298 K . Units are $0.001 \AA$.


Fig. 5. Relationship between temperature and the length of the $b$ axis.

Fig. 6 displays difference thermal ellipsoids calculated as $U_{i j}$ (Diff. $)=U_{U}\left(T_{1}\right)-U_{i j}\left(T_{2}\right)$, which show the reduction of thermal motion for each atom between temperatures $T_{1}$ and $T_{2}$. These difference thermal motions apparently are quite reasonable for all atoms. Fig. 7 shows the relationship between temperature and the magnitude of each of the six $U_{i j}$ classes, which seems to be quite linear in the low-temperature region. From Fig. 7, it is apparent that $U_{22}, U_{12}$ and $U_{23}$ classes which are related to motions perpendicular to the molecular plane are more reduced at low temperature than are $U_{11}, U_{33}$ and $U_{13}$ which represent motions in the molecular plane. Using the slopes for each $U_{i j}$ class from Fig. 7, it is possible to extrapolate $U$ values for $T=0 \mathrm{~K}$. These values are $79 \cdot 3,72 \cdot 5,78 \cdot 1,85 \cdot 7,78 \cdot 7$ and $67.4 \%$ of $U_{i j}$ at 35 K for $U_{11}, U_{22}, U_{33}, U_{12}, U_{13}$, and $U_{23}$ respectively. A second procedure was used to
extrapolate the thermal parameters to 0 K using individual second-order polynomials to represent $U_{i j}$ for each atom as a function of temperature, with the three coefficients determined by a least-squares procedure. Extrapolated $U_{i j}$ values at 0 K obtained in this fashion are listed in Table 6 and the corresponding ellipsoids are drawn in Fig. 8. These parameters provide estimates of the combined effects of zero-point motion and static disorder. The $U_{i j}(T=0 \mathrm{~K})$ values in Table 6 have been subjected to rigid-body thermalmotion analyses, and results of these calculations are included in Table 5.

The observed differences in bond distances with temperature (Fig. 2) are quite easily explained in terms of foreshortening due to rigid-body libration, except in the case of the intramolecular hydrogen bond. Estimates of the average magnitudes of these corrections for

## Table 5. Summary of rigid-body thermal-motion analyses

The units for mean-square amplitude of translational vibration ( $\mathbf{T}$ ), libration vibration ( $\mathbf{L}$ ), and root-mean-square fit $\left\langle\Delta U^{2}\right\rangle^{1 / 2}$ are 0.0001 $\AA^{2}, 0.0001 \mathrm{rad}^{2}$ and $0.0001 \AA^{2}$ respectively.

| Model* | Temperature | $T_{X}$ | $T_{Y}$ | $T_{z}$ | $L_{X}$ | $L_{Y}$ | $L_{z}$ | $\left\langle\Delta U^{2}\right\rangle^{1 / 2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\stackrel{Y}{\uparrow}$ | 298 K | 181 | 137 | 250 | 63 | 64 | 24 | 41 |
| $1<$ | 100 | 83 | 59 | 64 | 27 | 26 | 11 | 30 |
| (1) $\longrightarrow$ | 80 | 76 | 52 | 49 | 25 | 23 | 10 | 30 |
| $\xrightarrow{ }$ | 35 | 57 | 37 | 22 | 21 | 18 | 8 | 30 |
| - | 0 | 44 | 25 | 3 | 18 | 15 | 6 | 30 |
| ${ }^{Y}$ | 298 | 169 | 132 | 257 | 52 | 63 | 20 | 31 |
|  | 100 | 73 | 57 | 91 | 15 | 19 | 6 | 10 |
| (2) | 80 | 64 | 52 | 80 | 12 | 15 | 5 | 8 |
| (2) $\bigcirc$ | 35 | 46 | 38 | 59 | 7 | 9 | 3 | 6 |
| N | 0 | 32 | 29 | 46 | 4 | 4 | 2 | 5 |
|  | 298 | 180 | 135 | 227 | 74 | 44 | 28 | 32 |
| 1 | 100 | 84 | 56 | 33 | 44 | 23 | 15 | 27 |
| (3) | 80 | 77 | 50 | 18 | 42 | 21 | 14 | 28 |
| (3) $\bigcirc$ | 35 | 57 | 37 | -9 | 38 | 18 | 12 | 27 |
| C | 0 | 43 | 27 | -28 | 36 | 15 | 11 | 28 |
|  | 298 | 167 | 134 | 316 | 38 | 24 | 20 | 4 |
|  | 100 | 72 | 58 | 110 | 10 | 8 | 5 | 3 |
| ${ }^{\text {c }}$ | 80 | 63 | 53 | 96 | 7 | 6 | 4 | 3 |
| (4) $\bigcirc \longrightarrow X$ | 35 | 44 | 39 | 70 | 3 | 3 | 3 | 2 |
| $\mathrm{N}_{\mathrm{C}}$ | 0 | 30 | 30 | 52 | 0 | 0 | 2 | 3 |
| $Y$ | 298 | 154 | 160 | 337 | 226 | 52 | 32 | 6 |
| O (2) | 100 | 59 | 77 | 115 | 59 | 17 | 11 | 2 |
| (5) $\longrightarrow X$ | 80 | 52 | 69 | 100 | 52 | 12 | 9 | 2 |
| $\longrightarrow X(1)$ | 35 | 39 | 49 | 72 | 40 | 5 | 5 | 2 |
| O(1) | 0 | 31 | 34 | 54 | 37 | -1 | 3 | 3 |
| $Y$ | 298 | 151 | 169 | 332 | 296 | 35 | 29 | 8 |
|  | 100 | 76 | 59 | 113 | 91 | 10 | 9 | 4 |
| (6) $x$ (2) | 80 | 71 | 50 | 98 | 76 | 7 | 7 | 3 |
| $\longrightarrow x(2)$ | 35 | 52 | 34 | 72 | 53 | 2 | 4 | 3 |
| O(3) | 0 | 38 | 24 | 57 | 39 | -2 | 2 | 3 |

[^5]distances are given in Table 7. No significant changes are found for bond angles.

Displacements from the least-squares plane through the six non-hydrogen atoms of the pyridine ring are shown in Fig. 9. Significant changes in these displacements with temperature are observed for the carboxyl groups, where the librations around the $\mathrm{C}-\mathrm{C}$ bonds are very much reduced when the crystal is cooled, as can be seen from the $L_{X}$ values for these groups given in Table 5.

When the D-QNA crystal is cooled to 100 K or below, the intramolecular hydrogen-bond distance $\mathrm{O}(2) \cdots \mathrm{O}(3)$ increases very slightly $(0.006-0.008 \AA)$, and $D(5)$ moves approximately $0.008 \AA$ closer to the midpoint of the hydrogen bond, compared to the structure at 298 K . In the $\mathrm{N}(1)-\mathrm{D}(4) \cdots \mathrm{O}(4)-\mathrm{C}(8)$ hydrogen bond, there is a slight but possibly significant contraction of $0.02 \AA$ in the $\mathrm{D}(4) \cdots \mathrm{O}(4)$ distance upon cooling to 100 K or below (Fig. 2). However, part of this change can be traced to the foreshortening of the $\mathrm{N}(1)-\mathrm{D}(4)$ and $\mathrm{O}(4)-\mathrm{C}(8)$ bond distances at 298 K , which is adequately accounted for by the effects of rigid-body libration.

(a)

(c)

(b)

(d)

Fig. 6. Difference thermal ellipsoids calculated as $U_{i j}=U_{i j}\left(T_{1}\right)-$ $U_{U}\left(T_{2}\right) .(a) T_{1}=298 \mathrm{~K}, T_{2}=35 \mathrm{~K}$, (b) $T_{1}=100 \mathrm{~K}, T_{2}=35 \mathrm{~K}$, (c) $T_{1}=80 \mathrm{~K}, T_{2}=35 \mathrm{~K}$ and (d) $T_{1}=100 \mathrm{~K}, T_{2}=80 \mathrm{~K}$. Ellipsoids are drawn as in Fig. 1.


Fig. 7. Relationship between the temperature and average magnitude of each $U_{U}$ class. $R U_{U}(T)$ is calculated as follows: $R U_{i j}(T)=\sum U_{j u}(T) U_{U}(298) / \sum U_{U j}(298)^{2}$.

## Isotope effects

As can be seen by inspection of Table 1, the cell dimensions of H-QNA and D-QNA at both 100 and 298 K are very similar. Possibly significant differences are found in the $a$ axis $(0.008 \AA)$ at 100 K and the $b$ axis $(0.010 \AA)$ at 298 K . The differences in bond distances between D-QNA and H-QNA are shown in

Table 6. Extrapolated $U_{i j}$ values at $T=0 \mathrm{~K}$ calculated as a second-order polynomial function of temperature $(T): U_{i j}(T)=a T^{2}+b T+c$

Individual coefficients $a, b$ and $c$ for each atom were fitted by a leastsquares procedure using $U_{i j}$ values at the four different temperatures. For all atoms, the magnitude of $a$ is of the order of one per cent that of $b$, or less.

|  | $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{12}$ | $U_{13}$ | $U_{23}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
|  | 0.0034 | 0.0061 | 0.0029 | 0.0002 | 0.0018 | 0.0000 |
| $\mathrm{~N}(1)$ | 0.0005 |  |  |  |  |  |
| $\mathrm{C}(2)$ | 0.0036 | 0.0054 | 0.0028 | 0.0005 | 0.0016 | 0.0005 |
| $\mathrm{C}(3)$ | 0.0030 | 0.0057 | 0.0024 | 0.0001 | 0.0010 | -0.0001 |
| $\mathrm{C}(4)$ | 0.0031 | 0.0064 | 0.0031 | -0.0001 | 0.0013 | 0.0001 |
| $\mathrm{C}(5)$ | 0.0043 | 0.0071 | 0.0019 | 0.0001 | 0.0009 | 0.0002 |
| $\mathrm{C}(6)$ | 0.0042 | 0.0068 | 0.0031 | 0.0003 | 0.0016 | 0.0002 |
| $\mathrm{C}(7)$ | 0.0042 | 0.0051 | 0.0031 | 0.0000 | 0.0020 | -0.0001 |
| $\mathrm{C}(8)$ | 0.0041 | 0.0051 | 0.0037 | -0.0003 | 0.0023 | -0.0004 |
| $\mathrm{O}(1)$ | 0.0052 | 0.0097 | 0.0048 | 0.0008 | 0.0030 | 0.0002 |
| $\mathrm{O}(2)$ | 0.0042 | 0.0087 | 0.0032 | 0.0005 | 0.0015 | 0.0002 |
| $\mathrm{O}(3)$ | 0.0041 | 0.0096 | 0.0033 | 0.0005 | 0.0018 | 0.0007 |
| $\mathrm{O}(4)$ | 0.0047 | 0.0086 | 0.0043 | -0.0002 | 0.0029 | 0.0008 |
| $\mathrm{H}(1)$ | 0.0159 | 0.0315 | 0.0166 | 0.0061 | 0.0117 | -0.0001 |
| $\mathrm{H}(2)$ | 0.0172 | 0.0291 | 0.0077 | 0.0021 | 0.0039 | 0.0013 |
| $\mathrm{H}(3)$ | 0.0096 | 0.0296 | 0.0156 | -0.0001 | 0.0045 | 0.0005 |
| $\mathrm{D}(4)$ | 0.0115 | 0.0164 | 0.0117 | 0.0007 | 0.0076 | 0.0005 |
| $\mathrm{D}(5)$ | 0.0109 | 0.0163 | 0.0098 | 0.0003 | 0.0022 | 0.0017 |



Fig. 8. Extrapolated structure at $T=0 \mathrm{~K}$, with ellipsoids drawn as in Fig. 1 and calculated from $U_{i j}$ values given in Table 6.


Fig. 9. Displacements from the least-squares plane through the six non-hydrogen atoms of the pyridine ring at 35 K . Changes in displacements (displacement at $T$ - displacement at 35 K ) for $T=80,100$ and 298 K , respectively, are given below the value at 35 K . Units are $0.001 \AA$.

Fig. 4. As expected, substantial differences are found in the $N(1)-D(4), O(2)-D(5)$, and $O(3)-D(5)$ bonds. In addition, significant differences are observed for the distances $\mathrm{C}(7)-\mathrm{O}(1), \mathrm{C}(8)-\mathrm{O}(3)$ and $\mathrm{C}(6)-\mathrm{H}(3)$.

A summary of the effects of $D$ substitution on the geometry of the hydrogen bonds is given in Table 8. In the $O(2) \cdots D(5) \cdots O(3)$ system, when the $H$ is replaced by $D$, it moves approximately $0.025 \AA$ towards $O(3)$. On the other hand, in the $N(1)-D(4) \cdots O(4)$ system, replacement of the $H$ by $D$ causes it to move approximately $0.016 \AA$ in a direction perpendicular to the $\mathrm{N}(1) \cdots \mathrm{O}(4)$ vector, thus decreasing slightly the $N(1)-D(4) \cdots O(4)$ angle and increasing the $N(1)-D(4)$ and $D(4) \cdots O(4)$ distances. The $\mathrm{O}(2) \cdots \mathrm{O}(3)$ and $\mathrm{N}(1) \cdots \mathrm{O}(4)$ distances exhibit no significant change upon deuteration. As can be seen from Fig. 4 and Table 8, the isotope effects observed in this study are found to be independent of temperature, in agreement with the generally accepted interpretation of these effects as a zero-point energy phenomenon (Robertson \& Ubbelohde, 1939). A similar conclusion has been reached by Thomas, Tellgren \& Olovsson (1974), in an X-ray diffraction study of $\mathrm{KHCO}_{3}$ and $\mathrm{KDCO}_{3}$. This structure exhibits hydrogen-bonded dimers of $\mathrm{HCO}_{3}^{-}$ions related by a center of symmetry, and the $\mathrm{O} \cdots \mathrm{O}$ distances are found to be significantly longer in $\mathrm{KDCO}_{3}$ than in $\mathrm{KHCO}_{3}$. (The magnitude of this effect is $0.022,0.021$, and $0.015 \AA$ at 298,219 and 95 K respectively.) By contrast, in quinolinic acid

Table 7. Average corrections ( $\AA$ ) to bond distances for the effects of rigid-body libration

the $\mathrm{O}(2) \cdots \mathrm{O}(3)$ and $\mathrm{N}(1) \cdots \mathrm{O}(4)$ distances show no significant change upon deuteration. This observation is perhaps not too surprising, since the $O(2) \cdots O(3)$ hydrogen bond is subject to intramolecular constraints, and the $N(1) \cdots O(4)$ bond is of moderate strength. Thomas (1972) has indicated that $\mathrm{O} \cdots \mathrm{O}$ bonds longer than $2.6 \AA$ may be expected to show no expansion with deuteration, although cooperative effects complicate the situation in crystals exhibiting networks of hydrogen bonds, as noted by Delaplane \& Ibers (1969). In ammonium oxalate monohydrate (Taylor \& Sabine, 1972) no significant increase in $\mathrm{N} \cdot . \mathrm{O}$ distances was found upon deuteration, for the $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ hydrogen bonds.

Systematic differences are observed between the thermal parameters of H-QNA and D-QNA at both 100 and 298 K . However, these differences are reduced to quite small values for all atoms except $D(4)$ and $\mathrm{D}(5)$ if the parameters in each $U_{i j}$ class are rescaled using the ratios defined in Table 9. These observed differences in thermal parameters may be caused by a random slipping of the molecular sheets with respect to one another, which might be expected to occur to a different extent in each crystal. This hypothesis is supported by the fact that the ratio for $U_{22}$ is close to $1 \cdot 0$. The differences in thermal parameters of D and H atoms persist even after rescaling, as is reflected in the principal axes of vibration listed in Table 10 and shown graphically in Fig. 10. These differences presumably are caused by the isotopic substitution. In each case the mean-square displacements for $D$ are less than those for H at the same temperature, as one would expect.

## Scattering lengths of N and D

The neutron scattering length of N has been refined at each temperature and the values obtained are 0.921 (4), 0.920 (4), 0.919 (4), and $0.922(4) \times 10^{-11}$ mm at $35,80,100$ and 298 K respectively. The deviations from the mean value of $0.921(2) \times 10^{-11}$ mm are within one estimated standard deviation. This result is actually somewhat smaller than the value of

Table 8. Comparison of the hydrogen-bond geometries in H-QNA and D-QNA at 100 and 298 K
(A) $\mathrm{N}(1)-\mathrm{H}(4) \cdots \mathrm{O}(4)-\mathrm{C}(8)$

|  | $\mathrm{N}(1)-\mathrm{H}(4)$ | $\mathrm{H}(4) \cdots \mathrm{O}(4)$ | $\mathrm{O}(4)-\mathrm{C}(8)$ | $\mathrm{N}(1) \cdots \mathrm{O}$ (4) | $\angle \mathrm{N}(1)-\mathrm{H}(4) \cdots \mathrm{O}(4)$ | $\angle \mathrm{H}(4) \cdots \mathrm{O}(4)-\mathrm{C}(8)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 K (H) | 1.039 (3) $\AA$ | 1.829 (4) A | 1.228 (3) $\AA$ | 2.710 (3) A | 140.2 (2) ${ }^{\circ}$ | 130.8 (2) ${ }^{\circ}$ |
| 100 (D) | 1.049 (1) | 1.835 (1) | 1.229 (1) | 2.715 (2) | 139.0 (1) | 130.7 (1) |
| 298 (H) | 1.036 (4) | 1.845 (4) | 1.222 (3) | 2.725 (2) | 140.5 (2) | 131.5 (2) |
| 298 (D) | 1.043 (2) | 1.854 (2) | 1.218 (2) | 2.730 (2) | 139.2 (1) | 131.0 (1) |
| (B) $\mathrm{C}(7)-\mathrm{O}(2) \cdots \mathrm{H}(5) \cdots \mathrm{O}(3)-\mathrm{C}(8)$ |  |  |  |  |  |  |
|  | $\mathrm{O}(2) \cdots \mathrm{H}(5)$ | $\mathrm{H}(5) \cdots \mathrm{O}(3)$ | $\mathrm{O}(2) \cdots \mathrm{O}(3)$ | $\angle \mathrm{O}(2) \cdots \mathrm{H}(5) \cdots \mathrm{O}(3)$ | $\angle \mathrm{C}(7)-\mathrm{O}(2) \cdots \mathrm{H}(5)$ | $\angle \mathrm{H}(5) \cdots \mathrm{O}(3)-\mathrm{C}(8)$ |
| 100 K (H) | 1.227 (3) $\AA$ | $1 \cdot 176$ (3) $\AA$ | 2.400 (2) $\AA$ | 174.5 (2) ${ }^{\circ}$ | $111.8(2)^{\circ}$ | 112.4 (2) ${ }^{\circ}$ |
| 100 (D) | 1.253 (2) | 1.150 (2) | 2.401 (2) | 175.2 (1) | 111.9 (1) | 112.5 (1) |
| 298 (H) | 1.238 (5) | 1.163 (5) | 2.398 (3) | 174.4 (4) | 111.4 (4) | 112.7 (4) |
| 298 (D) | 1.257 (2) | 1.138 (2) | 2.393 (2) | 175.2 (2) | 112.1 (1) | 112.9 (1) |

$0.936 \times 10^{-11} \mathrm{~mm}$ recently given by Koester (1977), but agrees well with $0.917(9) \times 10^{-11} \mathrm{~mm}$, an average value taken from several other structure refinements based upon single-crystal data (Kvick et al., 1974). In this context, the value of $0.941(5) \times 10^{-11}$ mm obtained for H-QNA at 100 K (Takusagawa \& Koetzle, 1978) appears to be somewhat larger than normal.

The two D scattering lengths were also allowed to vary in the refinements. The refined values are lower than the normal value of $b_{\mathrm{D}}=0.6672 \times 10^{-11} \mathrm{~mm}$

Table 9. Ratios of thermal parameters of D-QNA and H-QNA
$R U_{i j}=\Sigma U_{i j}(\mathrm{D}) U_{i j}(\mathrm{H}) / \Sigma U_{i j}(\mathrm{H})^{2}$, where the summation extends over all atoms except $H(4)$ and $H(5)$.

| Temperature | $R U_{11}$ | $R U_{22}$ | $R U_{33}$ | $R U_{12}$ | $R U_{13}$ | $R U_{23}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 K | 0.9108 | 0.9822 | 0.8277 | 0.7853 | 0.6675 | 0.8815 |
| 298 | 0.8286 | 0.9747 | 0.8913 | 0.7452 | 0.8006 | 1.0424 |

Table 10. Principal axes of vibration for D and H atoms
Mean-square

displacement* $\quad l \quad$| Direction cosines $\dagger$ |  |
| :---: | :---: |
|  | $m$ |

(a) 100 K

| $U_{11}$ | $\mathrm{H}(4)$ | 0.0346 | -0.0032 | 0.9942 | 0.1076 |
| :--- | :--- | ---: | ---: | ---: | ---: |
|  | $\mathrm{D}(4)$ | 0.0279 | -0.0195 | 0.9959 | 0.0883 |
| $U_{22}$ | $\mathrm{H}(4)$ | 0.0228 | 0.3588 | -0.9993 | 0.9281 |
|  | $\mathrm{D}(4)$ | 0.0188 | -0.1026 | -0.0898 | 0.9907 |
| $U_{33}$ | $\mathrm{H}(4)$ | 0.0141 | 0.9334 | 0.0416 | -0.3563 |
|  | $\mathrm{D}(4)$ | 0.0101 | 0.9945 | 0.0104 | 0.1040 |
| $U_{11}$ | $\mathrm{H}(5)$ | 0.0394 | 0.4105 | 0.9103 | -0.0540 |
|  | $\mathrm{D}(5)$ | 0.0338 | 0.2983 | 0.9484 | -0.1075 |
| $U_{22}$ | $\mathrm{H}(5)$ | 0.0230 | 0.9118 | -0.4092 | 0.0344 |
|  | $\mathrm{D}(5)$ | 0.0222 | 0.9543 | -0.2946 | 0.0500 |
| $U_{33}$ | $\mathrm{H}(5)$ | 0.0200 | -0.0092 | 0.0633 | 0.9980 |
|  | $\mathrm{D}(5)$ | 0.0131 | -0.0138 | 0.1178 | 0.9929 |
| $(b)$ | 298 K |  |  |  |  |
| $U_{11}$ | $\mathrm{H}(4)$ | 0.0768 | -0.0059 | 0.9946 | 0.1037 |
|  | $\mathrm{D}(4)$ | 0.0630 | 0.0344 | 0.9993 | -0.0172 |
| $U_{22}$ | $\mathrm{H}(4)$ | 0.0413 | 0.0388 | -0.1035 | 0.9939 |
|  | $\mathrm{D}(4)$ | 0.0375 | -0.1955 | -0.0569 | 0.9791 |
| $U_{33}$ | $\mathrm{H}(4)$ | 0.0204 | 0.9992 | 0.0100 | -0.0383 |
|  | $\mathrm{D}(4)$ | 0.0170 | 0.9807 | -0.0063 | 0.1955 |
| $U_{11}$ | $\mathrm{H}(5)$ | 0.0919 | 0.2994 | 0.9524 | -0.0571 |
|  | $\mathrm{D}(5)$ | 0.0895 | 0.2525 | 0.9639 | -0.0847 |
| $U_{22}$ | $\mathrm{H}(5)$ | 0.0441 | 0.9489 | -0.3033 | -0.0871 |
|  | $\mathrm{D}(5)$ | 0.0435 | 0.9670 | -0.2544 | -0.0122 |
| $U_{33}$ | $\mathrm{H}(5)$ | 0.0306 | 0.1002 | 0.0280 | 0.9946 |
|  | $\mathrm{D}(5)$ | 0.0232 | 0.0332 | 0.0788 | 0.9963 |

[^6]


Fig. 10. Comparison of thermal parameters of $\mathrm{H}-\mathrm{QNA}$ and D QNA for atoms involved in hydrogen bonds. Values for H-QNA have been rescaled using the ratios given in Table 9. (a) $\mathrm{N}-\mathrm{H} \ldots$ O at 100 K , (b) $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ at 298 K , (c) $\mathrm{O} \cdots \mathrm{H} \cdots \mathrm{O}$ at 100 K , (d) $\mathrm{O} \cdots \mathrm{H} \cdots \mathrm{O}$ at 298 K . The direction of view is approximately parallel to the plane of the pyridine ring.

Table 11. Deuterium scattering lengths ( $\times 10^{-11} \mathrm{~mm}$ ) and calculated percentage occupancy of protons

|  | $D(4)$ |  | $D(5)$ |  |
| :---: | :---: | :---: | :---: | :---: |
| Temperature | Scattering <br> length | H (\%) | Scattering <br> length | H (\%) |
| 35 K | $0.641(4)$ | $2.6(4)$ | $0.620(4)$ | $4.6(4)$ |
| 80 | $0.640(4)$ | $2.6(4)$ | $0.619(4)$ | $4.7(4)$ |
| 100 | $0.641(4)$ | $2.6(4)$ | $0.622(4)$ | $4.4(4)$ |
| 298 | $0.636(4)$ | $3.0(3)$ | $0.624(4)$ | $4.2(4)$ |

(Shull, 1972), thus indicating that a small percentage of H remains at these sites as shown in Table 11. The contamination by H may be due to an insufficient number of recrystallizations for complete exchange, or, more likely, it may indicate that the $\mathrm{D}_{2} \mathrm{O}$ used in this study was impure. The difference in percentage of H between the $\mathrm{D}(4)$ and $\mathrm{D}(5)$ sites is significant judging from the e.s.d.'s.

The relationship between the H:D exchange ratio and hydrogen-bonding environment has been studied using nearly a null-matrix with respect to the H,D atoms in $a$-oxalic acid dihydrate (Coppens, 1970) and ammonium oxalate monohydrate (Taylor \& Sabine, 1972). These studies indicate that the protons show a definite preference for the site which participates in the short $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bond in oxalic acid, and for the water molecules relative to the ammonium ions in ammonium oxalate monohydrate. In a $50 \%$ deuterated sample of yttrium oxalate trihydrate, which contains an $\mathrm{H}_{5} \mathrm{O}_{2}^{+}$ion and an additional water molecule that forms no hydrogen bonds, the protons are found to occupy preferentially the central position in the $\mathrm{H}_{5} \mathrm{O}_{2}^{+}$ion (Brunton \& Johnson, 1975). In deuterated decaborane a higher percentage of residual H was found at bridged, than at terminal positions (Tippe \& Hamilton, 1969) while in a partially deuterated sample of $\mathrm{H}_{2} \mathrm{Os}_{3}(\mathrm{CO})_{10} \mathrm{CH}_{2}$, the H was found to occupy preferentially the bridging osmium hydride positions and
the D the methylene-group sites (Calvert, Shapley, Schultz, Williams, Suib \& Stucky, 1978). The proton occupancies for D-QNA given in Table 11 are in accord with the observations cited above, and with simple energy considerations, which imply that the $D$ atoms should prefer the sites with deepest potential wells. It is tempting to speculate that the slightly more equal distribution of protons at 298 K compared to that at the lower temperatures may be due to an entropy contribution. A similar tendency toward more equal $\mathrm{H}: \mathrm{D}$ ratios at higher temperatures was observed in yttrium oxalate trihydrate where the sensitivity was enhanced owing to the use of an overall D fraction of $0 \cdot 5$. However, in the present study this temperaturedependent effect lies at the $1 \sigma$ level and is of marginal significance.

We wish to thank Joseph Henriques for technical assistance, and Philip Coppens, Franz Reidinger, and Jacques Verbist for helpful discussions.

## References

Alcock, N. W. (1970). Crystallographic Computing, edited by F. R. Ahmed, pp. 271-278. Copenhagen: Munksgaard.
Bacon, G. E. (for Neutron Diffraction Commission) (1972). Acta Cryst. A28, 357-358.

Becker, P. J. \& Coppens, P. (1975). Acta Cryst. A31, 417425.

Brunton, G. D. \& Johnson, C. K. (1975). J. Chem. Phys. 62, 3797-3806.
Busing, W. R., Martin, K. O. \& Levy, H. A. (1962). ORFLS. Report ORNL-TM-305. Oak Ridge National Laboratory, Tennessee.
Calvert, R. B., Shapley, J. R., Schultz, A. J., Williams, J. M., Suib, S. L. \& Stucky, G. D. (1978). J. Am. Chem. Soc. 100, 6240-6241.
Coppens, P. (1970). Thermal Neutron Diffraction, edited by B. T. M. Willis, pp. 82-100. Oxford Univ. Press.

Delaplane, R. G. \& Ibers, J. A. (1969). Acta Cryst. B25, 2423-2437.
Dimmler, D. G., Greenlaw, N., Kelley, M. A., Potter, D. W., Rankowitz, S. \& Stubblefield, F. W. (1976). IEEE Trans. Nucl. Sci. NS-23, 398-405.
Hamilton, W. C. (1965). Acta Cryst. 18, 502-510.
Johnson, C. K. (1969). Acta Cryst. A25, 187-194.
Johnson, C. K. (1970a). Chemistry Division Annual Progress Report ORNL-4581, pp. 133-134. Oak Ridge National Laboratory, Tennessee.
Johnson, C. K. (1970b). ORJFLS. Unpublished work.
Johnson, C. K. (1976). ORTEP-II. Report ORNL-5138. Oak Ridge National Laboratory, Tennessee.
Koester, L (1977). Neutron Physics, edited by L. Koester \& A. Steyerl, p. 36. Berlin, Heidelberg, New York: Springer.
K vick, $\AA$ (1978). Private communication.
Kvick, Ả., Koetzle, T. F., Thomas, R. \& Takusagawa, F. (1974). J. Chem. Phys. 60, 3866-3874.

McMullan, R. K., Andrews, L. C., Koetzle, T. F., Reidinger, F., Thomas, R. \& Williams, G. J. B. (1976). NEXDAS. Neutron and $X$-ray Data Acquisition System. Unpublished work.
Meulenaer, J. de \& Tompa, H. (1965). Acta Cryst. 19, 1014-1018.
Robertson, J. M. \& Ubbelohde, A. R. (1939). Proc. R. Soc. London Ser. A, 170, 222-240, 241-251.
Schomaker, V. \& Trueblood, K. N. (1968). Acta Cryst. B24, 63-76.
Shull, C. G. (1972). Private communication.
Takusagawa, F., Hirotsu, K. \& Shimada, A. (1973). Bull. Chem. Soc. Jpn, 46, 2372-2380.
Takusagawa, F. \& Koetzle, T. F. (1978). Acta Cryst. B34, 1149-1154.
Taylor, J. C. \& Sabine, T. M. (1972). Acta Cryst. B28, 3340-3351.
Templeton, D. H. \& Templeton, L. K. (1973). Am. Crystallogr. Assoc. Meeting, Storrs, Connecticut. Abstract E10.
Thomas, J. O. (1972). Acta Cryst. B28, 2037-2045.
Thomas, J. O., Tellgren, R. \& Olovsson, I. (1974). Acta Cryst. B30, 1155-1166.
Tippe, A. \& Hamilton, W. C. (1969). Inorg. Chem. 8, 464-470.

Acta Cryst. (1979). B35, 2135-2140

# 4-Octadecynoic Acid, a Largely Regular Structure in Space Group Pī 

By Frode Mo<br>Institutt for røntgenteknikk, Universitetet i Trondheim-NTH, N-7034 Trondheim-NTH, Norway

(Received 11 April 1979; accepted 21 May 1979)


#### Abstract

$\mathrm{C}_{18} \mathrm{H}_{32} \mathrm{O}_{2}$ is triclinic ( $P \overline{1}$ ) with $a=8.71(2), b=$ 5.475 (10), $c=45.13$ (7) $\AA ; \alpha=92.55$ (15), $\beta=$ $93.15(15), \gamma=123.95(25)^{\circ}, Z=4$. The structure

0567-7408/79/092135-06\$01.00


which has some OD character was solved in two discrete steps by direct and Patterson methods. Fullmatrix least-squares refinement based on $1155 F_{o}$ from visually estimated film intensities was terminated at $R$ $=0.071$. In the ordered structure, neighbouring (c) 1979 International Union of Crystallography


[^0]:    * Research carried out at Brookhaven National Laboratory under contract with the US Department of Energy and supported by its Division of Basic Energy Sciences.
    $\dagger$ To whom correspondence should be addressed.

[^1]:    * For data collection at room temperature ( 298 K ), the crystal was sealed in a glass capillary and mounted directly on the diffractometer.

[^2]:    * Calibration of the refrigerator by observation of the magnetic phase transition in $\mathrm{FeF}_{2}$ at 78.4 K indicated that the actual sample temperatures are within 2 K of these recorded values.

[^3]:    * Lists of structure factors obtained at $35,80,100$ and 298 K have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34465 ( 42 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CHI 2HU, England.

[^4]:    * The notation D-QNA and H-QNA will be used here to indicate respectively quinolinic acid recrystallized from $\mathrm{D}_{2} \mathrm{O}$, and ordinary undeuterated quinolinic acid.

[^5]:    * Coordinate systems used in these calculations are indicated by the arrows $\rightarrow X$ and $\rightarrow Y$. The $Z$ coordinate is taken in the direction perpendicular to the page. For models (1)-(4), the $\mathbf{S}$ tensor was included in the calculations, and the results transformed to place the origin at the center of reaction. For models (5) and (6), the origin was fixed at the ring $C$ atom, and the $\mathbf{S}$ tensor was not included.

[^6]:    * Mean-square displacements are in $\AA^{2}$, and those for H atoms have been rescaled using the ratios given in Table 9.
    $\dagger$ Defined relative to the following bases: for $\mathrm{H}, \mathrm{D}(4), X_{1}$ is along $\mathrm{N}(1)-\mathrm{H}, \mathrm{D}(4), X_{2}$ lies in the ac plane and $X_{3}$ is normal to $X_{1}$ and $X_{2}$; for $\mathrm{H}, \mathrm{D}(5), X_{1}$ is along $\mathrm{O}(2) \cdots \mathrm{O}(3), X_{2}$ lies in the ac plane and $X_{3}$ is normal to $X_{1}$ and $X_{2}$.

